

Theoretical Analysis of Resonant Mode Splitting in A Single Microfiber Knot-Ring Resonator

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Abstract—In this paper, we established a theoretical model and made an analysis of single knot-ring resonator by polarization transmission matrix. The theoretical analysis shows that two orthogonal polarization modes of knot-ring, which are originally resonant at the same wavelength, will be split into two resonant modes at two different wavelengths. The mode splitting owes to the twisted coupler of the knot-ring, which makes these two orthogonal polarization modes couple each other. This results can provide a novel method to implement coupled-resonator-induced transparency in a single knot-ring.

Keywords—microfiber; resonator; knot-ring; coupled-resonator-induced transparency;

I. INTRODUCTION

Optical microfibers have been intriguing due to its strong confinement of light in the micro or nano scale[2-5], leading to enhancement of the interaction with material and the sensitivity to its environment. Of all devices based on microfiber, the ring-like resonator is most intriguing. Recently, a simple and low-cost method are reported to fabricate optical resonator, i.e. knot-ring resonator by a single microfiber[2]. Many devices based on the knot-ring resonator are also reported, such as sensors[6,7], a lasers[8], an all optical tunable filter[9]. For all these devices, the resonant mode of the knot-ring is vital. However, it is not reported before that the resonant mode splitting can be induced by the twist coupler of a knot-ring. In this paper, the theoretical model of a knot-ring is established by transmission matrix method, and the resonant mode splitting due to coupling of two polarization modes is analyzed.

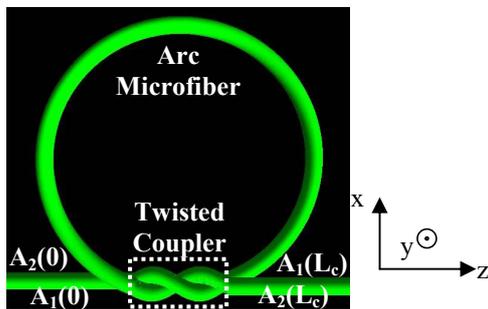


Fig. 1. Schematic of theoretical model of a knot-ring resonator constructed by a single micro-fiber

II. THEORETICAL MODEL OF A KNOT-RING RESONATOR

In this section, the theoretical model of a knot-ring resonator is established. As shown in Fig.1, this knot-ring resonator is usually composed of two parts, one is a twisted coupler and other an arc segment of micro-fiber.

According to the coupling mode theory of K. Morishita[10] the output E-field components $[a_{ix'}, a_{iy'}]$ in rotated coordinates can be represented by the input $[a_{ix}, a_{iy}]$ in laboratorial coordinates for the twisted coupler.

$$\begin{bmatrix} a_{1x'}(L_c) \\ a_{1y'}(L_c) \\ a_{2x'}(L_c) \\ a_{2y'}(L_c) \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} & t_{13} & t_{14} \\ -t_{12} & t_{22} & -t_{14} & t_{24} \\ t_{13} & t_{14} & t_{11} & t_{12} \\ -t_{14} & t_{24} & -t_{12} & t_{22} \end{bmatrix} \cdot \begin{bmatrix} a_{1x}(0) \\ a_{1y}(0) \\ a_{2x}(0) \\ a_{2y}(0) \end{bmatrix} \exp(-i\beta L_c), \quad (1)$$

On the other hand, the transmission Jones matrix through the arc microfiber in knot-ring can be given by,

$$\mathbf{A}_2(0) = \alpha \exp(-i\beta L_r) \cdot \mathbf{A}_1(L_c), \quad (2)$$

where α is total loss coefficient after a circular propagation, and L_r is length of the arc microfiber. As shown in Fig.1, $\mathbf{A}_1(L_c) = [a_{1x}(L_c), a_{1y}(L_c)]$ and $\mathbf{A}_2(0) = [a_{1x}(0), a_{1y}(0)]$ are respectively the input and the output E-field amplitudes of the twisted coupler of the knot-ring. The propagation constant of the arc microfiber $\beta = 2\pi n_{\text{eff}}/\lambda$.

By rewriting the Eq.(1) in sub-matrix form and substituting Eq.(2) in it, the transmission equation of knot-ring resonator can be obtained in matrix form,

$$\mathbf{A}_2(L_c) = \mathbf{T} \cdot \mathbf{A}_1(0), \quad (3)$$

where \mathbf{T} is the transmission matrix of the knot-ring,

$$T_{xx} = T_{yy}, \quad T_{xy} = -T_{yx}. \quad (4)$$

During the above deduction, the rotational transform of E-field components was done from rotated coordinates to laboratorial coordinates.

III. RESULTS AND DISCUSSIONS

In the below, a practical case is considered that the total twisting angle θ is not exactly equal to 2π , and can be written as $\theta = 2\pi + \delta\theta$. In this case, a knot-ring has a radius of $a = 60\mu\text{m}$, $L_R = 2\pi a$, effective refractive index $n_{\text{eff}} = 1.4$, and circular loss coefficient $\alpha = 0.98$, and the coupling coefficient of the twisted

coupler is of $\kappa=0.9799$. The transmissions t_{xy} and t_{xx} are deduced by using transmission matrix \mathbf{T} in Eq.(3) and Eq.(4) when the input E_x -field $A_1(0)=[1,0]$ is launched without E_y -field. The transmission spectrum of t_{xx} and t_{yx} for the knot-ring can be obtained, which are shown in Fig.2 and Fig.3 respectively.

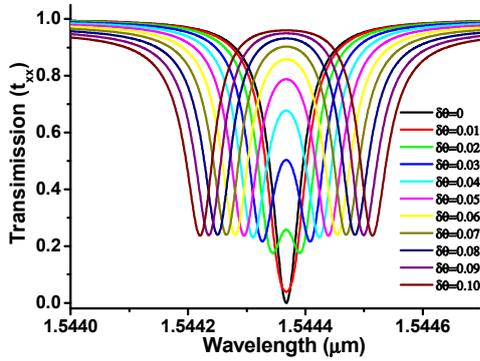


Fig. 2. Transmission spectra t_{xx} of the knot-ring under different values of $\delta\theta$, where t_{xx} denotes the normalized transmission to include only x polarization mode.

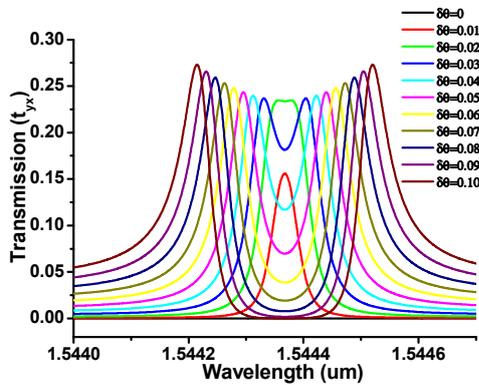


Fig. 3. Transmission spectra t_{yx} of the knot-ring under different values of $\delta\theta$, where t_{yx} denotes the normalized transmission to y polarization mode.

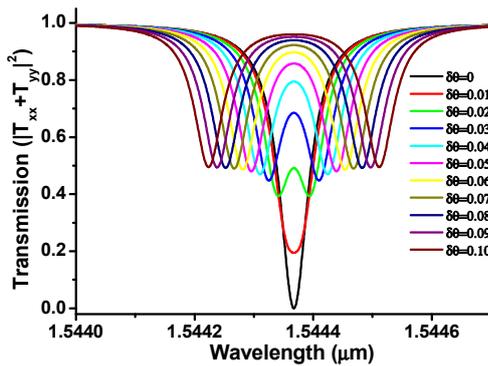


Fig. 4. Total transmission spectra $|T_{xx} + T_{yx}|^2$ of the knot-ring under different values of $\delta\theta$, where $|T_{xx} + T_{yx}|^2$ denotes the total normalized transmission contributed both by x and y polarization field.

Both Fig.2 and Fig.3 show that the deviation $\delta\theta$ of twist angle from 2π leads to the coupling between x and y polarization resonant mode in the knot-ring, and thus resonant

mode splitting which is analogous to the mode splitting induced by two coupled resonators[11], i.e. coupled-resonator-induced transparency. Fig. 3 also shows that transmission of the E_y -field without initial energy reaches the maximum at the resonant wavelength. This separation of the two split modes can be tuned by $\delta\theta$. All these twisting angles are in radian unit. It is important to notice that an evident resonant mode splitting can be observed only when $\delta\theta$ is large enough. In this case, $\delta\theta$ should not be less than 0.02rad as shown in Fig.2. This large $\delta\theta$ can be achieved in practical experiment by rotating the knot-ring around the microfiber that constitutes it.

The total transmission spectrum $|T_{xx} + T_{yx}|^2$ through the knot-ring, i.e. the spectrum measured by optical spectrum analyzer, are shown in Fig.5. It shows that the absorption at resonant wavelength with mode splitting, i.e. $\delta\theta \neq 0$, becomes shallower than that with polarization mode coupling, i.e. $\delta\theta = 0$. It implies that the twist angle θ of the knot ring is also an essential factor that contributes to deterioration of the resonance.

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