

Time-domain simulation of semiconductor laser light with correlated amplitude and phase noise

Outline

- Motivation
- Physical principle
- Simulation algorithm
- Time-domain results
- Noise spectra
- Applications
- Conclusions

- **Motivation**

- Physical principle

- Simulation algorithm

- Time-domain results

- Noise spectra

- Applications

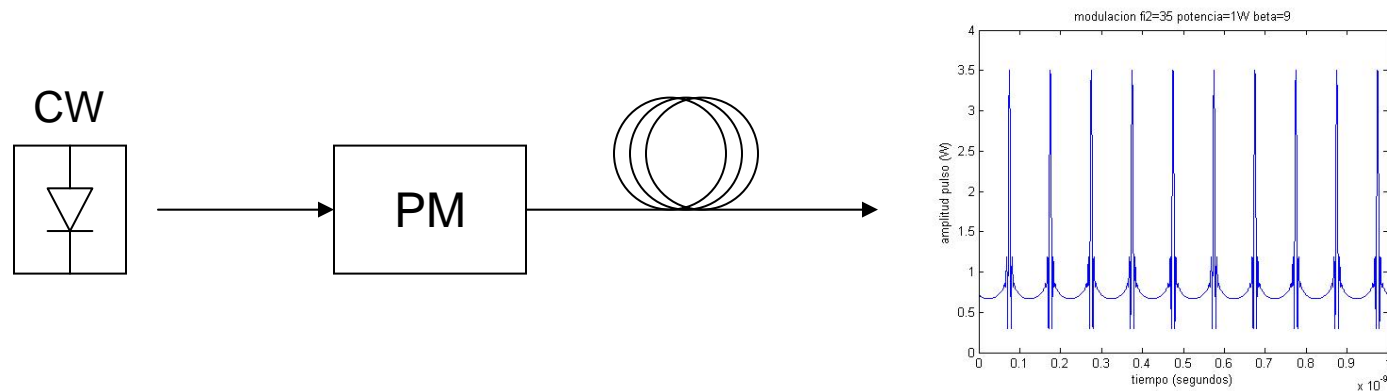
- Conclusions

Motivation

Frequency domain analysis is sufficient for LTI systems

$$|X(f)|^2 \longrightarrow \boxed{H(f)} \longrightarrow |H(f)X(f)|^2$$

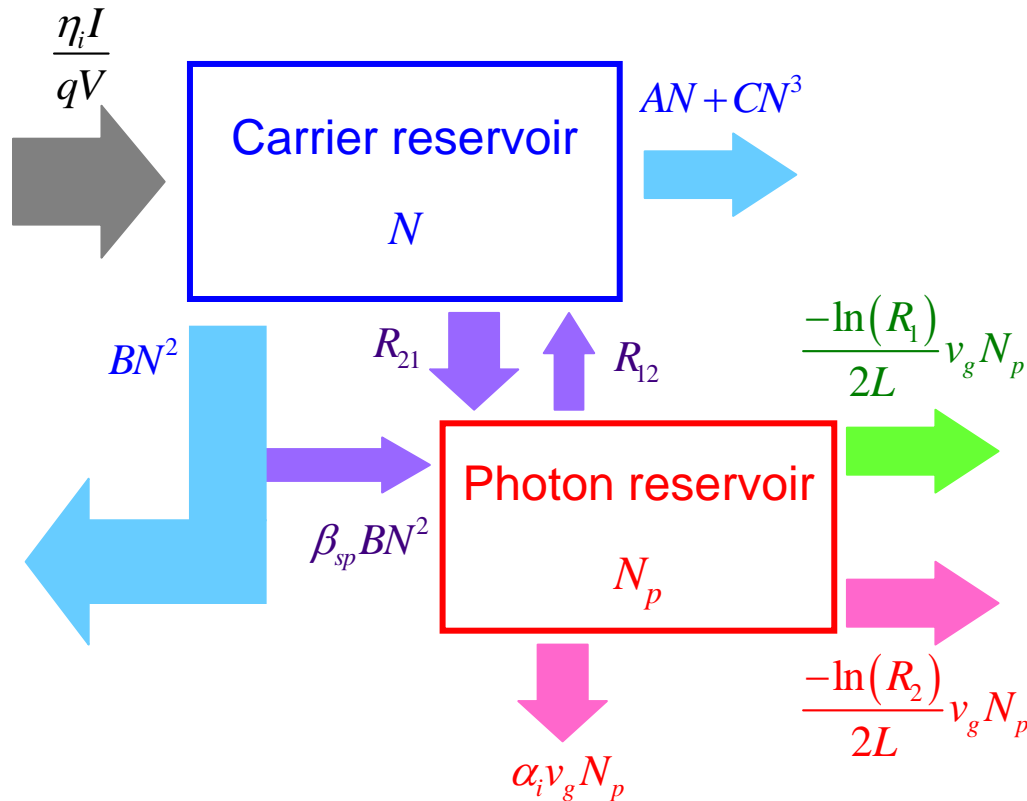
Increasing number of applications combine LTI and non-LTI subsystems



Correct system evaluation needs
time-domain noise characterization

-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

Noise Origin in Semiconductor Lasers



All processes are the sum of individual uncorrelated events

Noise is similar to white noise “colored” by the laser response

The lasing frequency depends on N through refractive index

Photon output adds partition noise

Spontaneously emitted photons add random phase

Rate Equations and Langevin Picture

$$\frac{dN}{dt} = \frac{\eta_i I}{qV} - AN - CN^3 - BN^2 - R_{21} + R_{12} + F_N$$

$$\frac{dN_p}{dt} = \Gamma R_{21} - \Gamma R_{12} + \Gamma \beta_{sp} BN^2 + \frac{\ln(R_1)}{2L} v_g N_p + \frac{\ln(R_2)}{2L} v_g N_p - \alpha_i v_g N_p + F_P$$

Related!!!

Output photon number

Langevin noise sources F_N and F_P represent randomness in the generation/loss processes (poissonian characteristics)

Effect of noise sources is analogous to substitution of rates with Poisson-distributed variables

-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

Computation of carrier and photon evolution

Approximation of evolution by numerically solving density rate equations as difference equations

$$N(t + \Delta t) = N(t) + x_I(t) - x_{nr}(t) - x_{sp}(t) - x_{21}(t) + x_{12}(t)$$

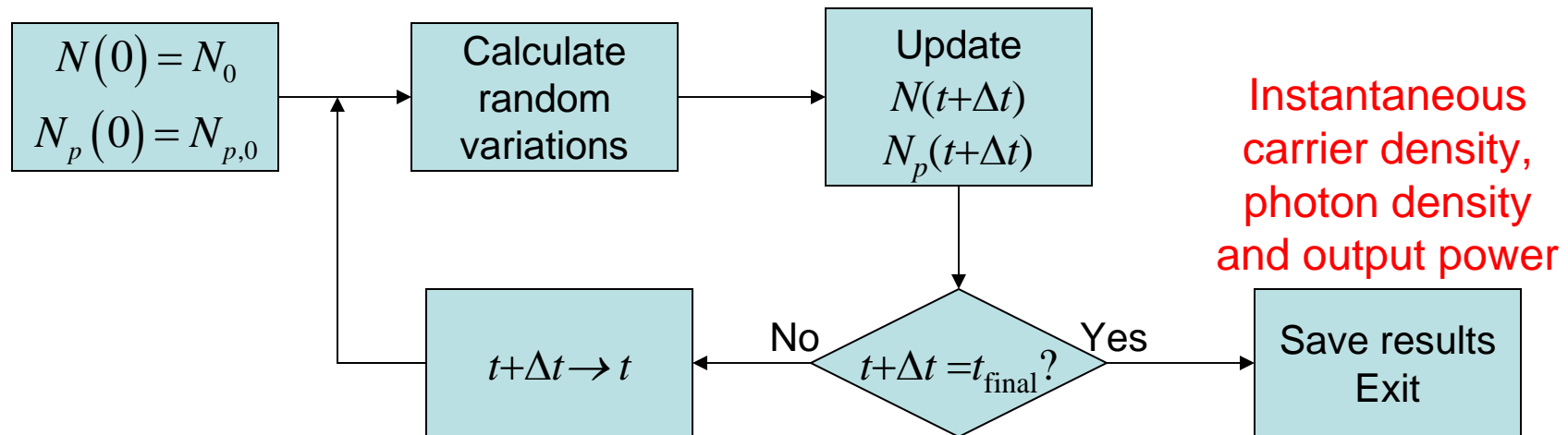
$$N_p(t + \Delta t) = N_p(t) + \Gamma x_{21}(t) - \Gamma x_{12}(t) + \Gamma \beta_{sp} x_{sp}(t) - x_{o1}(t) - x_{o2}(t) - x_l(t)$$

Instantaneous output power may be calculated using $P_{out}(t) = \frac{E_{ph} x_{o1}(t) V_p}{\Delta t}$

Allows the computation of instantaneous carrier and photon densities
Partition noise taken into account

Simulation Algorithm

Self-consistent solution to rate equations provides equilibrium point for given output power ($N_0, N_{p,0}$)



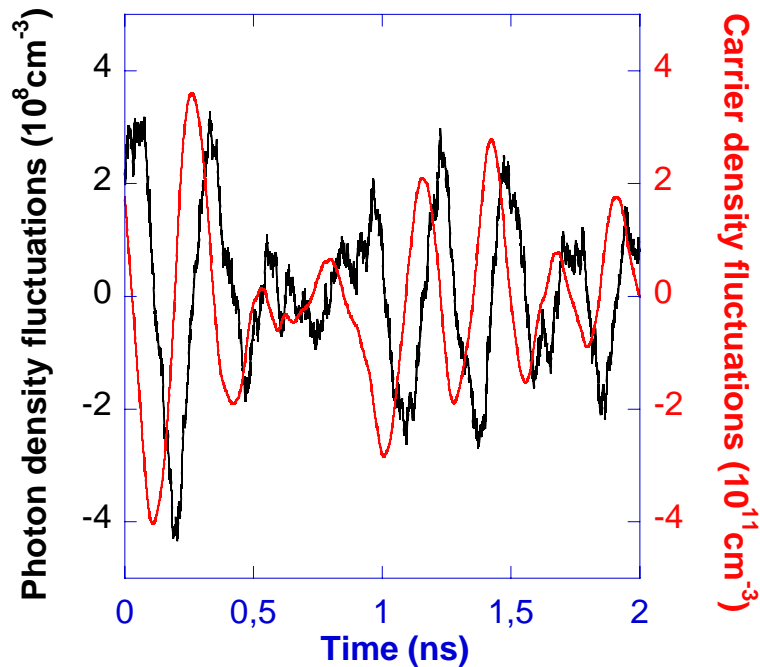
Phase noise due to spontaneous emission noise is added as random variable with gaussian probability distribution

$$\Delta f(t) = \frac{\alpha}{4\pi} \Gamma v_g a (N(t) - N_0) + x_\phi(t)$$

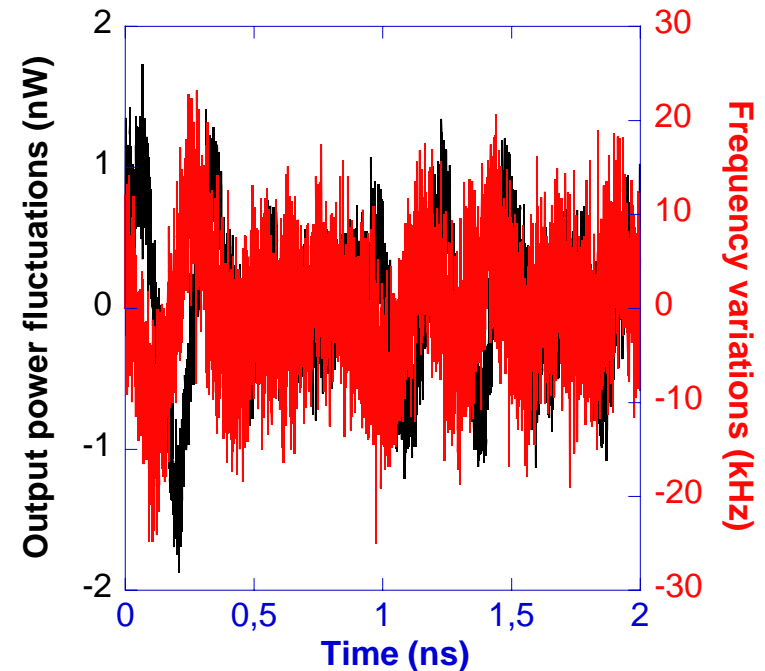
-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

Evolution of Output Power and Frequency

Simulated time evolution of carrier and photon density



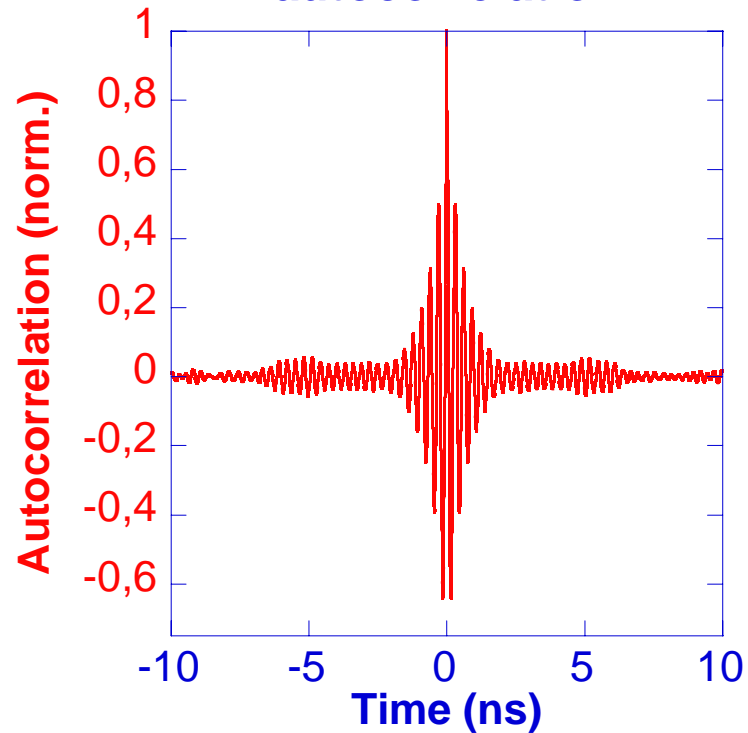
Simulated time evolution of output power and lasing frequency



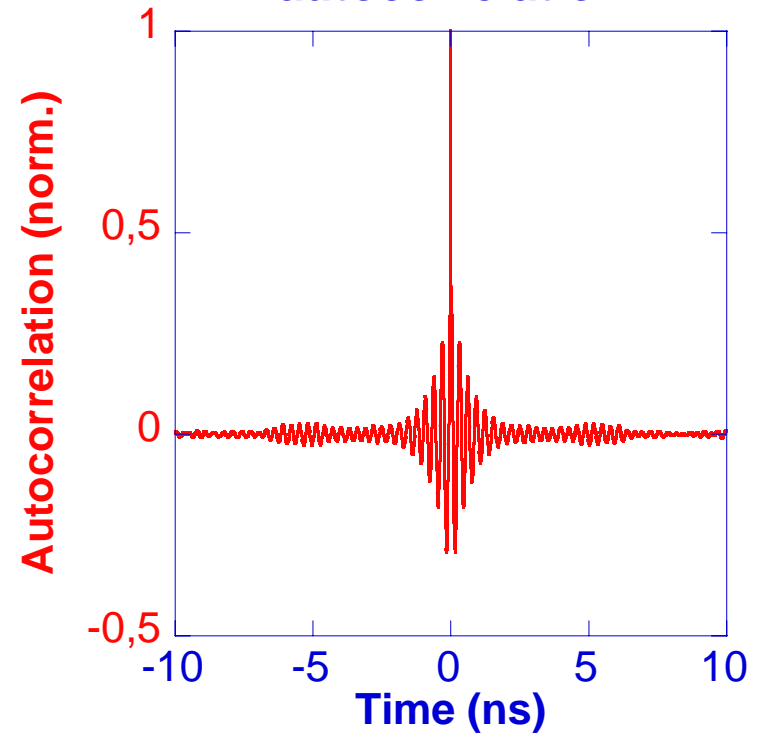
Visible correlation between amplitude and phase noise
Optical power variations trail frequency variations by about $\pi/2$

Autocorrelations

Output power fluctuations
autocorrelation



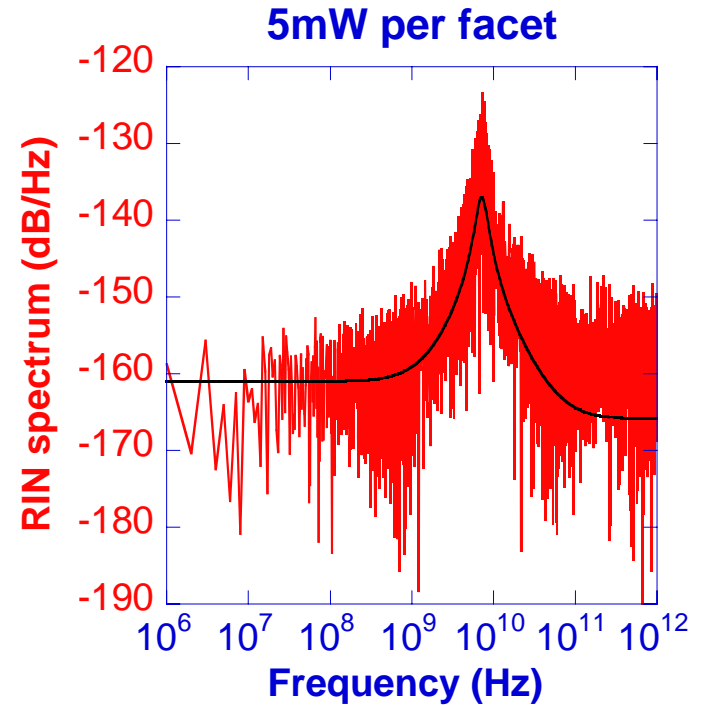
Lasing frequency fluctuations
autocorrelation



Partition noise makes the output power fluctuations autocorrelation “noisier”

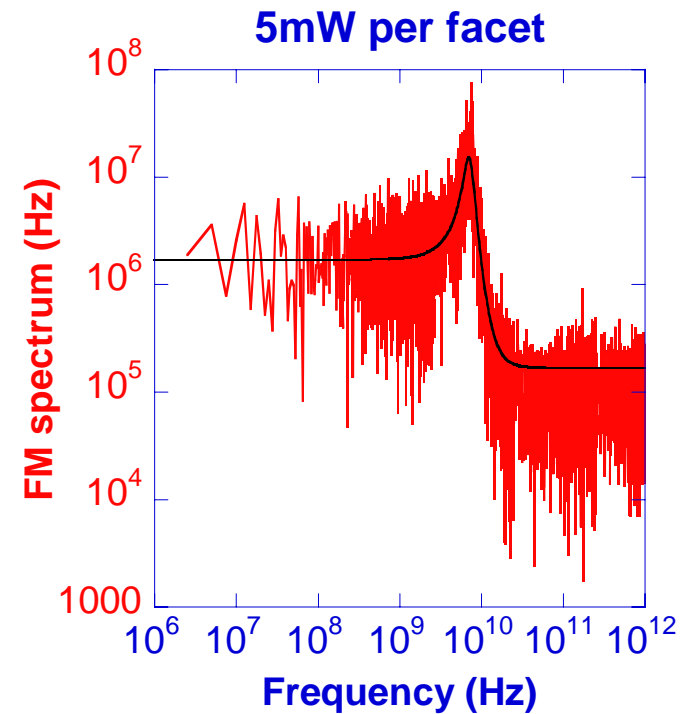
-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

RIN Spectra



Good agreement between computed results and
previously existing theoretical results

Frequency Noise Spectra

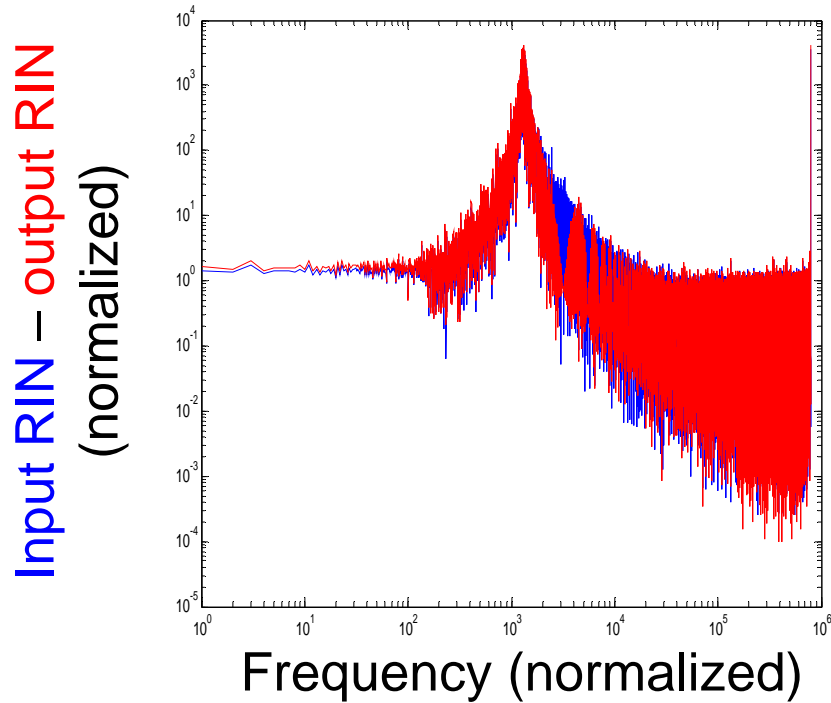


Good agreement between computed results and
previously existing theoretical results

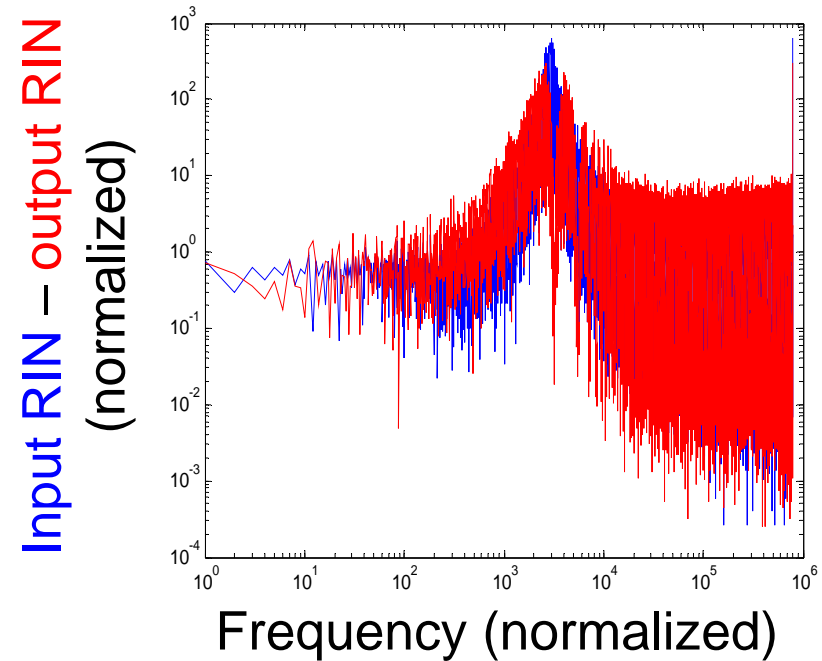
-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

RIN Reduction

1mW per facet

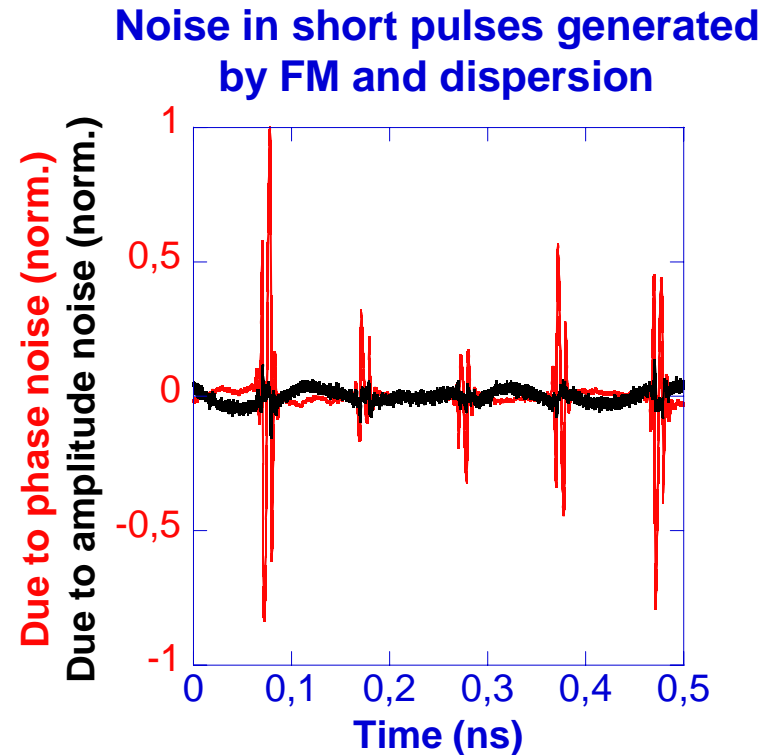
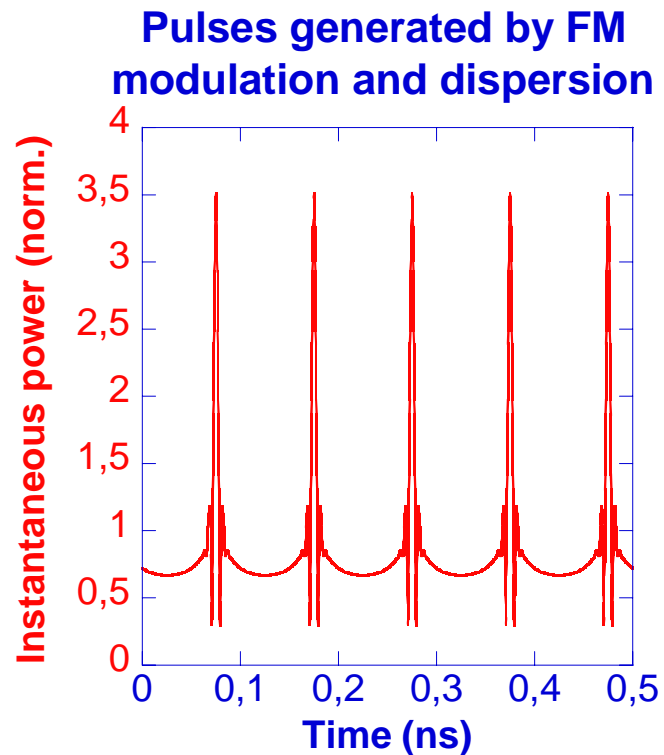


5mW per facet



Future work: check with existing theory (Vahala & Newkirk)

Noise in Short Pulses



Future work: Evaluate critical parameters and reduce noise

-
- Motivation
 - Physical principle
 - Simulation algorithm
 - Time-domain results
 - Noise spectra
 - Applications
 - Conclusions

Conclusions

- **Time-domain algorithm** that computes laser noise based on **physical principle** of operation
- **Correlation** ensured by use of coupled **density-rate equations**
- “Natural” introduction of **partition noise** – artificial introduction of **spontaneous emission** effect on phase noise
- Results **match predictions** from existing frequency-domain models
- Possible application to systems combining both **LTI and non-LTI** components